



TRANSPOWER

ELECTRICITY  
AUTHORITY  
TE MANA HIKO



# Reserve shortfall modelling using simplified worked examples



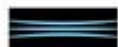
COMPETITION • RELIABILITY • EFFICIENCY

# Contents of this pack

These illustrative results were obtained using a simplified Excel model

The first section shows the flaws in using the current reserve deficit constraint model under RTP (ie, in trying to use 'real' CVP values)

The second section shows similar conditions using the risk-violation curves



TRANSPOWER

COMPETITION • RELIABILITY • EFFICIENCY



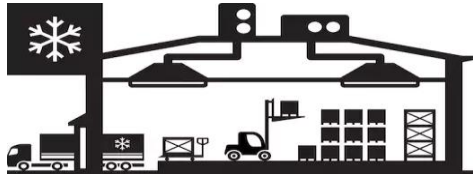
## Worked examples of the (failed) reserve deficit approach

# Market Scenario Example

one risk setter and both reserve classes constrained

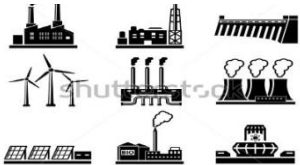
North Island

Demand : 1650 MW



IL FIR : 100 MW @ 100 \$/MWh

IL SIR : 100 MW @ 200 \$/MWh



ENRG: 1500MW @ 100\$/MWh

FIR : 200MW @ 20 \$/MWh

SIR : 250MW @ 30 \$/MWh



Ignoring transmission losses, net free reserve, HVDC ramp up, HVDC capacity, reserve sharing and reserve requirement in SI

Energy CVP = 10k

FIR CVP = 10k

SIR CVP = 10k

South Island

Demand : 1000 MW



ENRG: 3000MW @ 0.01\$/MWh

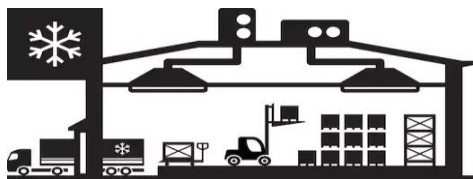


# Market Scenario Example

one risk setter and both reserve classes constrained

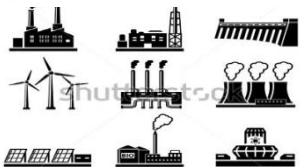
North Island

Demand : 1650 MW



IL FIR : 100 MW @ 100 \$/MWh → 100 MW

IL SIR : 100 MW @ 200 \$/MWh → 100 MW



Energy price: \$10k/MWh

FIR price: \$100/MWh

SIR price: \$9899.99/MWh

ENRG: 1500MW @ 100\$/MWh → 1300 MW

FIR : 200MW @ 20 \$/MWh → 200 MW

SIR : 250MW @ 30 \$/MWh → 200 MW



HVDC  
NI ← SI

300 MW

South Island

Demand : 1000 MW



ENRG: 3000MW @ 0.01\$/MWh  
→ 1300 MW

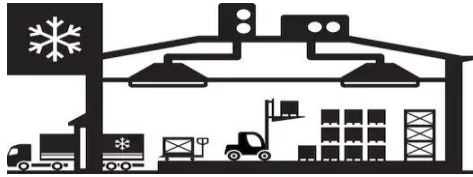


Energy shortage: 50 MW

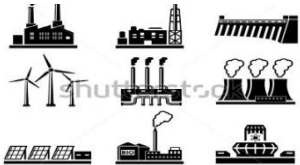
# Market Scenario Example

one risk setter and both reserve classes constrained

North Island  
Demand : 1650 MW



IL FIR : 100 MW @ 100 \$/MWh  
IL SIR : 100 MW @ 200 \$/MWh



ENRG: 1500MW @ 100\$/MWh  
FIR : 200MW @ 20 \$/MWh  
SIR : 250MW @ 30 \$/MWh



Ignoring transmission losses, net free reserve, HVDC ramp up, HVDC capacity, reserve sharing and reserve requirement in SI

Energy CVP = 10k  
FIR CVP = 4.5k  
SIR CVP = 4.5k

South Island  
Demand : 1000 MW



ENRG: 3000MW @ 0.01\$/MWh

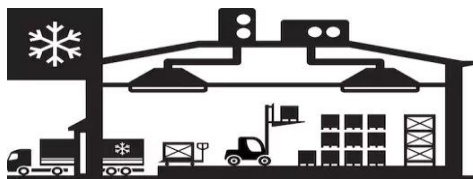


# Market Scenario Example

one risk setter and both reserve classes constrained

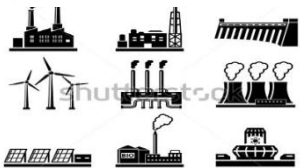
North Island

Demand : 1650 MW



IL FIR : 100 MW @ 100 \$/MWh → 100 MW

IL SIR : 100 MW @ 200 \$/MWh → 100 MW



Energy price: \$9,000.01/MWh

FIR price: \$4,500.00/MWh

SIR price: \$4,500.00/MWh

ENRG: 1500MW @ 100\$/MWh → 1300 MW

FIR : 200MW @ 20 \$/MWh → 200 MW

SIR : 250MW @ 30 \$/MWh → 200 MW

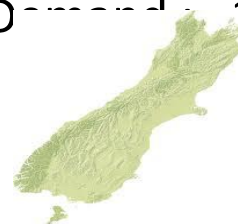


HVDC  
NI ← SI

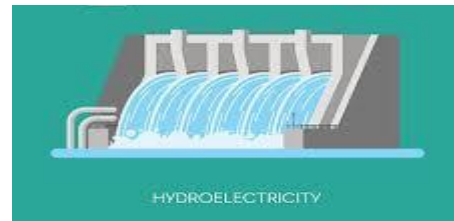
350 MW

South Island

Demand : 1000 MW



ENRG: 3000MW @ 0.01\$/MWh  
→ 1350 MW



**FIR/SIR shortage: 50 MW**



# Market Scenario Example

## three risk setters

### North Island

Demand : 1510 MW

ENRG: 350MW @ 0.01\$/MWh

FIR : 20MW @ 1\$/MWh

SIR : 30MW @ 1\$/MWh

ENRG: 350MW @ 0.02\$/MWh

FIR : 20MW @ 2\$/MWh

SIR : 30MW @ 2\$/MWh

ENRG: 100MW @ 5k\$/MWh

ENRG: 1000MW @ 100\$/MWh

FIR : 200MW @ 3\$/MWh

SIR : 300MW @ 3\$/MWh

Ignoring transmission losses, net free reserve, HVDC ramp up, HVDC capacity, reserve sharing and reserve requirement in SI

Energy CVP = 10k

FIR CVP = 10k

SIR CVP = 10k

### South Island

Demand : 1000 MW

ENRG: 3000MW @ 0.01\$/MWh





# Market Scenario Example

## FIR shortage: 10 MW

rs

North Island

Demand : 1510 MW

ENRG: 230MW @ 0.01\$/MWh

FIR : 20MW @ 1\$/MWh

SIR : 30MW @ 1\$/MWh

ENRG: 230MW @ 0.02\$/MWh

FIR : 20MW @ 2\$/MWh

SIR : 30MW @ 2\$/MWh

ENRG: 0MW @ 5k\$/MWh

Energy price: \$3334.35/MWh

FIR price: \$10k/MWh

SIR price: \$3/MWh

ENRG: 800MW @ 100\$/MWh

FIR : 200MW @ 3\$/MWh

SIR : 200MW @ 3\$/MWh

HVDC

NI ← SI

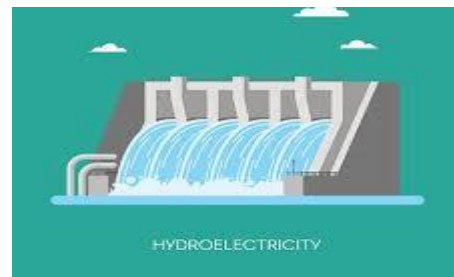
250 MW

South Island

Demand : 1000 MW



ENRG: 1250MW @ 0.01\$/MWh



# Market Scenario Example

## three risk setters

### North Island

Demand : 1510 MW

ENRG: 350MW @ 0.01\$/MWh

FIR : 20MW @ 1\$/MWh

SIR : 30MW @ 1\$/MWh

ENRG: 350MW @ 0.02\$/MWh

FIR : 20MW @ 2\$/MWh

SIR : 30MW @ 2\$/MWh

ENRG: 100MW @ 5k\$/MWh

ENRG: 1000MW @ 100\$/MWh

FIR : 200MW @ 3\$/MWh

SIR : 300MW @ 3\$/MWh

Ignoring transmission losses, net free reserve, HVDC ramp up, HVDC capacity, reserve sharing and reserve requirement in SI

Energy CVP = 10k

FIR CVP = 15k

SIR CVP = 15k

### South Island

Demand : 1000 MW



ENRG: 3000MW @ 0.01\$/MWh



# Market Scenario Example

## three risk setters

North Island

Demand : 1510 MW

ENRG: 220MW @ 0.01\$/MWh

FIR : 20MW @ 1\$/MWh

SIR : 30MW @ 1\$/MWh

ENRG: 220MW @ 0.02\$/MWh

FIR : 20MW @ 2\$/MWh

SIR : 30MW @ 2\$/MWh

ENRG: 30MW @ 5k\$/MWh

Energy price: \$5000/MWh

FIR price: \$14,996.96/MWh

SIR price: \$3/MWh

ENRG: 800MW @ 100\$/MWh

FIR : 200MW @ 3\$/MWh

SIR : 190MW @ 3\$/MWh

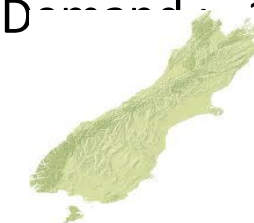
HVDC

NI ← SI

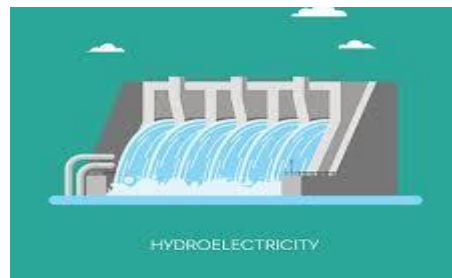
240 MW

South Island

Demand : 1000 MW



ENRG: 1240MW @ 0.01\$/MWh



## Worked examples of the risk-violation curve



# Market Scenario Example (1 risk setter – No shortfall)

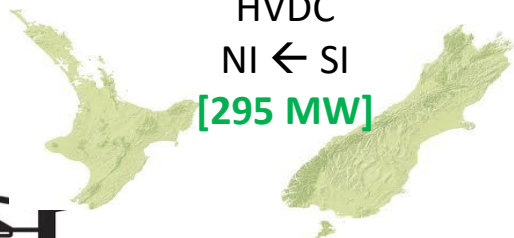
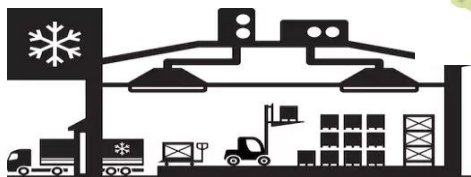
Ignoring transmission losses, net  
free reserve, HVDC ramp up,  
HVDC capacity, reserve sharing  
and reserve requirement in SI

NI demand  
**1595 MW**

HVDC  
NI  $\leftarrow$  SI

**[295 MW]**

SI demand  
1000 MW



ENRG: 3000MW @ 1\$/MWh  
**[1295 MW]**

IL FIR : 100 MW @ 100 \$/MWh **[95 MW]**

IL SIR : 100 MW @ 200 \$/MWh **[95 MW]**



**Energy price: \$301/MWh**

**FIR price: \$100/MWh**

**SIR price: \$200/MWh**

ENRG: 1500MW @ 100\$/MWh **[1300 MW]**

FIR : 200MW @ 20 \$/MWh **[200 MW]**

SIR : 250MW @ 30 \$/MWh **[200 MW]**

	CE Risk Shortage			Energy shortage	
	MW	FIR price	SIR price	MW	Price
1	10	4.5k	4.5k	80	10k
2	20	12.5k	12.5k	160	15k
3	100	17.5k	17.5k	1,3k	20k

The lowest cost supply of an additional MW in the NI would be via the HVDC @\$301/MWh (\$1/MWh + \$100/MWh + \$200/MWh). Reflected in the NI price.

Relationship between energy and reserve prices send consistent signals to market participants.

1MW offered into the energy market is more valuable than the same MW offered into NI FIR and/or SIR market.

# Market Scenario Example (1 risk setter – FIR risk shortfall)

Ignoring transmission losses, net  
free reserve, HVDC ramp up,  
HVDC capacity, reserve sharing  
and reserve requirement in SI

NI demand  
**1605** MW

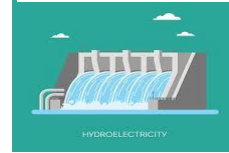
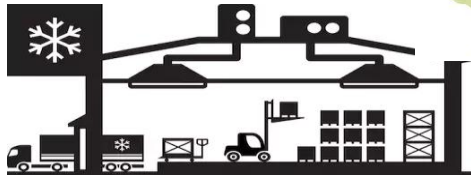
HVDC  
NI  $\leftarrow$  SI

SI demand  
1000 MW

**[305 MW]**

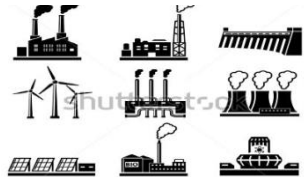
ENRG: 3000MW @ 1\$/MWh  
**[1305 MW]**

	CE Risk Shortage			Energy shortage	
	MW	FIR price	SIR price	MW	Price
1	10	<b>4.5k</b>	4.5k	80	10k
2	20	12.5k	12.5k	160	15k
3	100	17.5k	17.5k	1,3k	20k



IL FIR : 100 MW @ 100 \$/MWh **[100 MW]**  
IL SIR : **110** MW @ 200 \$/MWh **[105 MW]**

**Energy price: \$4,701/MWh**  
**FIR price: \$4,500/MW/h [5MW]**  
**SIR price: \$200/MW/h**



ENRG: 1500MW @ 100\$/MWh **[1300 MW]**  
FIR : 200MW @ 20 \$/MWh **[200 MW]**  
SIR : 250MW @ 30 \$/MWh **[200 MW]**

The lowest cost supply of an additional MW in the NI would be via the HVDC @\$4,701/MWh (\$1/MWh + \$4,500/MWh + \$200/MWh). Reflected in the NI price.

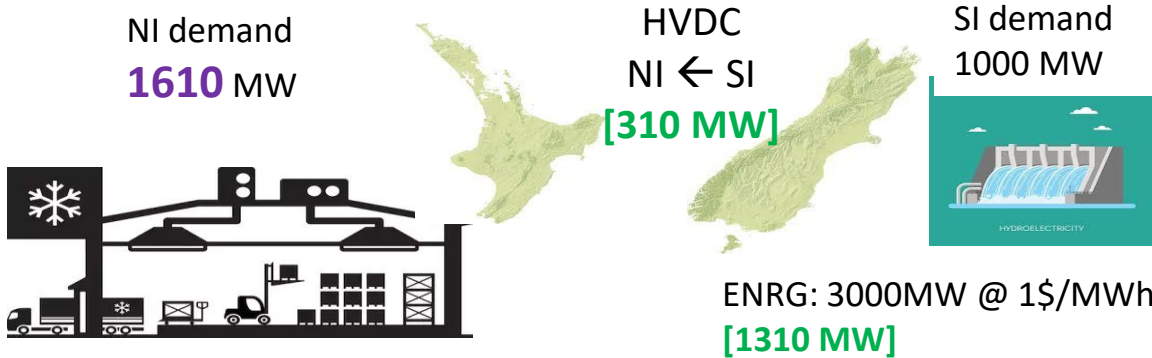
Relationship between energy and reserve prices send consistent signals to market participants.

A MW offered into the NI energy MW is more valuable than the same MW offered into the NI FIR and/or SIR market



# Market Scenario Example (1 risk setter – FIR and SIR risk shortfall)

Ignoring transmission losses, net free reserve, HVDC ramp up, HVDC capacity, reserve sharing and reserve requirement in SI



	CE Risk Shortage			Energy shortage	
	MW	FIR price	SIR price	MW	Price
1	10	<b>4.5k</b>	<b>4.5k</b>	80	10k
2	20	12.5k	12.5k	160	15k
3	100	17.5k	17.5k	1,3k	20k

IL FIR : 100 MW @ 100 \$/MWh **[100 MW]**  
IL SIR : 100 MW @ 200 \$/MWh **[100 MW]**



**Energy price: \$9,001/MWh**  
**FIR price: \$4,500/MWh [10MW]**  
**SIR price : \$4,500/MWh [10MW]**

ENRG: 1500MW @ 100\$/MWh **[1300 MW]**  
FIR : 200MW @ 20 \$/MWh **[200 MW]**  
SIR : 250MW @ 30 \$/MWh **[200 MW]**

The lowest cost supply of an additional MW in the NI would be via the HVDC @\$9,001/MWh (\$1/MWh + \$4,500/MWh + \$4,500/MWh). Reflected in the NI price.

Relationship between energy and reserve prices send consistent signals to market participants.

A MW offered into the NI energy MW is more valuable than the same MW offered into the NI FIR and/or SIR market



# Market Scenario Example (3 risk setter – No shortfall)

Ignoring transmission losses, net  
free reserve, HVDC ramp up,  
HVDC capacity, reserve sharing  
and reserve requirement in SI

NI demand  
**1580 MW**

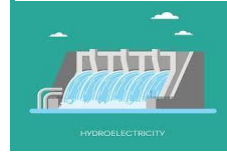


HVDC  
NI  $\leftarrow$  SI

**[240 MW]**



SI demand  
1000 MW



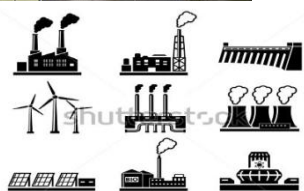
ENRG: 350MW @ 0.01\$/MWh **[220MW]**  
FIR : 20MW @ 1\$/MWh **[20MW]**  
SIR : 30MW @ 1\$/MWh **[30MW]**

ENRG: 3000MW @ 1\$/MWh  
**[1240 MW]**

ENRG: 220MW @ 0.02\$/MWh **[220MW]**  
FIR : 20MW @ 2\$/MWh **[20MW]**  
SIR : 30MW @ 2\$/MWh **[30MW]**

ENRG: 100MW @ 9.5k\$/MWh **[0MW]**

ENRG: 1100MW @ 100\$/MWh **[900MW]**  
FIR : 200MW @ 3\$/MWh **[200MW]**  
SIR : 300MW @ 3\$/MWh **[190MW]**



	CE Risk Shortage			Energy shortage	
	MW	FIR price	SIR price	MW	Price
1	10	4.5k	4.5k	80	10k
2	20	12.5k	12.5k	160	15k
3	100	17.5k	17.5k	1,3k	20k

Energy price: **\$100/MWh**  
FIR price: **\$296/MW/h**  
SIR price : **\$3/MW/h**

Marginal MW of FIR  $\sim$  3 x marginal MW of  
energy (reflects the increased impact of a  
marginal MW of reserve versus energy on the  
system at the optimal solution)

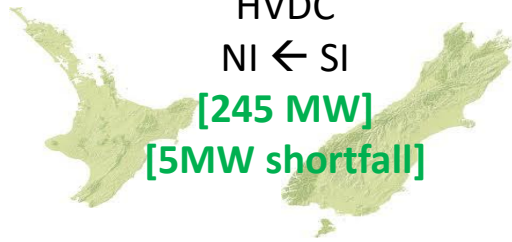
# Market Scenario Example (3 risk setter – FIR shortfall)

Ignoring transmission losses, net  
free reserve, HVDC ramp up,  
HVDC capacity, reserve sharing  
and reserve requirement in SI

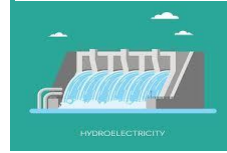
NI demand  
**1585 MW**



HVDC  
NI  $\leftarrow$  SI



SI demand  
1000 MW



ENRG: 350MW @ 0.01\$/MWh **[220MW]**  
FIR : 20MW @ 1\$/MWh **[20MW]**  
SIR : 30MW @ 1\$/MWh **[30MW]**

ENRG: 3000MW @ 1\$/MWh  
**[1241 MW]**

ENRG: 220MW @ 0.02\$/MWh **[220MW]**  
FIR : 20MW @ 2\$/MWh **[20MW]**  
SIR : 30MW @ 2\$/MWh **[30MW]**

ENRG: 100MW @ 9.5k\$/MWh **[0MW]**

ENRG: 1100MW @ 100\$/MWh **[900MW]**  
FIR : 200MW @ 3\$/MWh **[200MW]**  
SIR : 300MW @ 3\$/MWh **[190MW]**

	CE Risk Shortage			Energy shortage	
	MW	FIR price	SIR price	MW	Price
1	10	<b>4.5k</b>	4.5k	80	10k
2	20	12.5k	12.5k	160	15k
3	100	17.5k	17.5k	1,3k	20k

Energy price: **\$4501/MWh**  
FIR price: **\$13498/MW/h**  
SIR price : **\$3/MW/h**

Marginal MW of FIR  $\sim 3 \times$  marginal MW of  
energy (reflects the increased impact of a  
marginal MW of reserve versus energy on the  
system at the optimal solution)

# Market Scenario Example (3 risk setter – FIR + SIR shortfall)

Ignoring transmission losses, net free reserve, HVDC ramp up, HVDC capacity, reserve sharing and reserve requirement in SI

NI demand  
**1585** MW



ENRG: 350MW @ 0.01\$/MWh **[225MW]**  
**[5MW FIR and SIR shortfall]**

FIR : 20MW @ 1\$/MWh **[20MW]**

SIR : **20**MW @ 1\$/MWh **[20MW]**

ENRG: 220MW @ 0.02\$/MWh **[220MW]**

FIR : 20MW @ 2\$/MWh **[20MW]**

SIR : **20**MW @ 2\$/MWh **[20MW]**

ENRG: 100MW @ 9.5k\$/MWh **[0MW]**

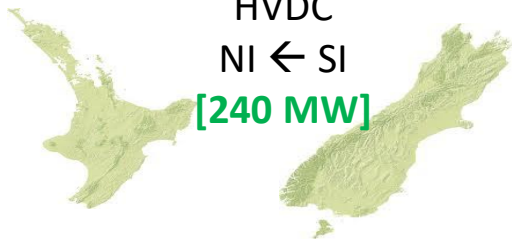
ENRG: 1100MW @ 100\$/MWh **[900MW]**

FIR : 200MW @ 3\$/MWh **[200MW]**

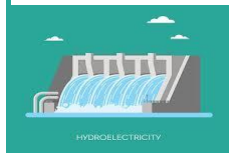
SIR : **200**MW @ 3\$/MWh **[200MW]**

HVDC  
NI ← SI

**[240 MW]**



SI demand  
1000 MW



ENRG: 3000MW @ 1\$/MWh  
**[1240 MW]**

	CE Risk Shortage			Energy shortage	
	MW	FIR price	SIR price	MW	Price
1	10	<b>4.5k</b>	<b>4.5k</b>	80	10k
2	20	12.5k	12.5k	160	15k
3	100	17.5k	17.5k	1,3k	20k

Energy price: **\$9000/MWh**

FIR price: **\$13499/MW/h**

SIR price : **\$13500/MW/h**

Price of marginal FIR and SIR risk shortage tranche reflected in energy price.

Marginal MW of energy can reduce FIR and SIR shortage (reflected in price)

Marginal MW of FIR and SIR can reduce FIR and SIR shortage costs by 3 (reflected in price)

