



Modelling reserve scarcity under RTP

EPOC Winter Workshop 2018

7th September 2018



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Current dispatch and pricing schedule

- Real time dispatch schedule used to dispatch energy and reserve.
- Real time pricing schedule produces indicative prices every five minute.
- Half-hourly based final price schedule define the settlement prices.
- Scarcity prices might be resolved during final prices.

Real time pricing

- Final pricing schedule cease to exist.
- Prices are defined according to real time dispatch.
- Half-hourly settlement prices defined by these “five-minute” prices
- Scarcity prices will remain and define the settlement prices.

Real time pricing – energy scarcity modelling

- 5% at \$10,000/MWh
- 15% at 15,000/MWh
- 80% at 20,000/MWh

Real time pricing – reserve scarcity modelling

- Current CVP for 6s (FIR) and 60s (SIR) reserve are \$100k/MWh
 - Under scarcity situation, load shedding instead of reserve may occur while energy is used to provide reserve.
- What are the right values of reserve CVPs?

Simplified risk/reserve modelling

HVDC risk :

$$\begin{aligned} \text{IslandRisk}_{i,c,rc} &= \text{HVDCRec}_i - \text{RiskOffset}_{i,c,rc} \\ \forall c \in \text{RESERVECLASSES} \forall i \in \text{ISLANDS} \forall rc \in \{\text{DCCE}_i, \text{DCECE}_i\} \end{aligned}$$

Generation risk :

$$\begin{aligned} \text{IslandRisk}_{i,c,rc} &= \text{Generation}_g - \text{RiskOffset}_{i,c,rc} + \text{Reserver}_g \\ \forall g \in \text{ISLANDRISKGENERATORS}_i \forall c \in \text{RESERVECLASSES} \\ \forall i \in \text{ISLANDS} \forall rc \in \{\text{ACCERISK}_i, \text{AECERISK}_i\} \end{aligned}$$

Simplified risk/reserve modelling

Matching of requirements and availability:

$$\begin{aligned} \text{IslandRisk}_{i,c,rc} &\leq \text{IslandReserve}_{i,c} + \textbf{ReserveDeficit}_{i,c} \\ \forall i \in \text{ISLANDS} \quad \forall c \in \text{RESERVECLASSES} \quad \forall rc \in \text{RISKCLASSES} \end{aligned}$$

Total cleared reserve:

$$\begin{aligned} \text{IslandReserve}_{i,c} &= \sum_{r \in \text{RESERVEOFFERS}_{i,c}} \text{Reserve}_r \\ \forall c \in \text{RESERVECLASS} \quad \forall i \in \text{ISLANDS} \end{aligned}$$

Simplified risk/reserve modelling

Objective function:

Net Benefit

$$\begin{aligned} &= \textit{DemandBenefit} - \textit{GenerationCosts} - \textit{ReserveCost} \\ &\quad - \textit{EnergyShortageCost} - \textit{ReserveDeficitCost} \\ &\quad - \textit{OtherViolationCost} \end{aligned}$$

Simplified risk/reserve modelling

$$EnergyShortageCost = \sum_{i,j} EnergyShortage_{i,j} \times EnergyCVP_j$$

$$ReserveDeficitCost = \sum_{i,c} ReserveDeficit_{i,c} \times ReserveCVP_c$$

$$\forall i \in ISLANDS \quad \forall j \in ENERGYSHORTAGEBLOCKS \quad \forall c \in RESERVECLASSES$$

SPD Energy and Reserve Price Basics

- Energy price: the marginal cost to supply the next 1 MW of demand.
- Reserve price: the benefit of 1 MW of “free” reserve to the system.
- Under normal situation, the definition of energy and reserve price is straight-forward.
- Under tight supply situation, the energy cost may impact reserve price and the reserve cost may impact energy price.

Potential issues with current reserve scarcity modelling

Case Study 1

Skip example

- One risk setter and both reserve classes constrained.
- The next 1 MW of demand supplied by a risk setting plant (or HVDC)

$$Price_{energy} = Cost_{energy} + Cost_{FIR} + Cost_{SIR}$$

- If scarcity occurs in both reserve market, virtual marginal cost of FIR and SIR is reserve CVP.

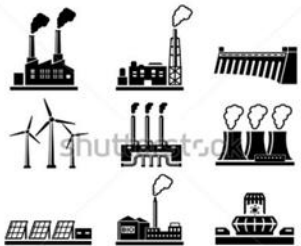
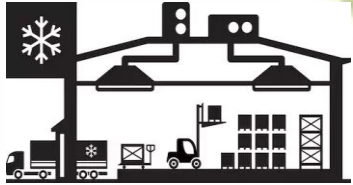
$$Price_{energy} = Cost_{energy} + CVP_{FIR} + CVP_{SIR}$$

- Assuming CVP_{FIR} and $CVP_{SIR} = \$10,000/\text{MWh}$
- $\rightarrow Price_{energy} > \$20k/\text{MWh} \rightarrow$ Load shedding is better option (Or is it?)

Case Study 1 example

North Island

Demand : 1650 MW



Ignoring transmission losses,
net free reserve, HVDC ramp
up, HVDC capacity, reserve
sharing and reserve
requirement in SI

Energy CVP = 10k

FIR CVP = 10k

SIR CVP = 10k

South Island

Demand : 1000 MW



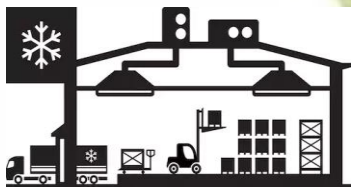
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Case Study 1 example

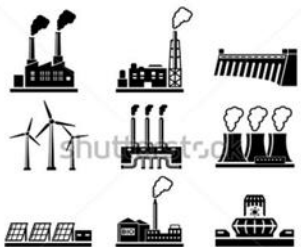
North Island

Demand : 1650 MW



IL FIR : 100 MW @ 100 \$/MWh

IL SIR : 100 MW @ 200 \$/MWh



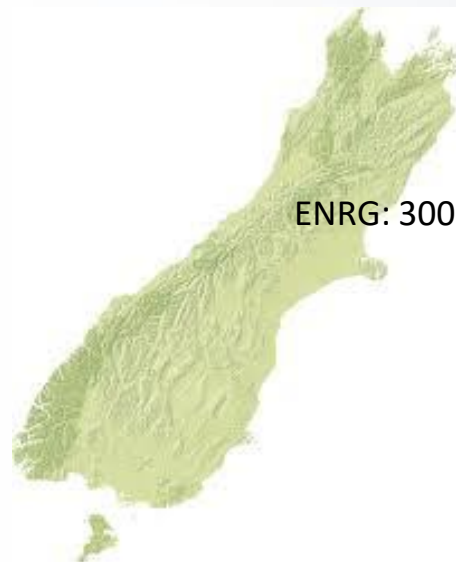
ENRG: 1500MW @ 100\$/MWh

FIR : 200MW @ 20 \$/MWh

SIR : 250MW @ 30 \$/MWh

South Island

Demand : 1000 MW



ENRG: 3000MW @ 0.01\$/MWh

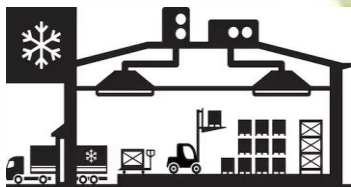


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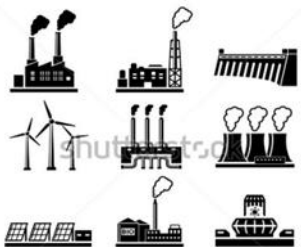
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Case Study 1 example

North Island
Demand : 1650 MW



IL FIR : 100 MW @ 100 \$/MWh
IL SIR : 100 MW @ 200 \$/MWh



ENRG: 1300 MW @ 100\$/MWh
FIR : 200 MW @ 20 \$/MWh
SIR : 200 MW @ 30 \$/MWh

HVDC
NI \leftarrow SI
300 MW

South Island
Demand : 1000 MW

ENRG: 1300 MW @ 0.01\$/MWh



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Case Study 1 example

North Island

Demand : 1650 MW

50 MW energy shortage



Energy price: \$10k/MWh

IL FIR : 100 MW @ 100 \$/MWh

IL SIR : 100 MW @ 200 \$/MWh

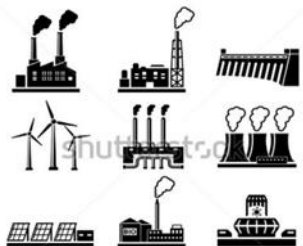
FIR price: \$100/MWh

SIR price: \$9899.99/MWh

ENRG: 1300 MW @ 100\$/MWh

FIR : 200 MW @ 20 \$/MWh

SIR : 200 MW @ 30 \$/MWh



HVDC
NI \leftarrow SI
300 MW

South Island

Demand : 1000 MW

ENRG: 1300 MW @ 0.01\$/MWh

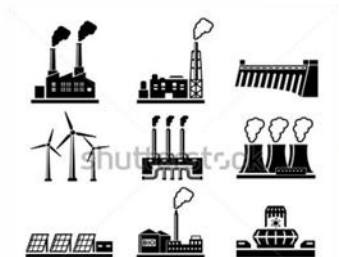
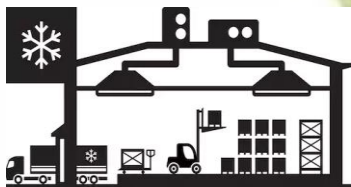


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Case Study 1 example

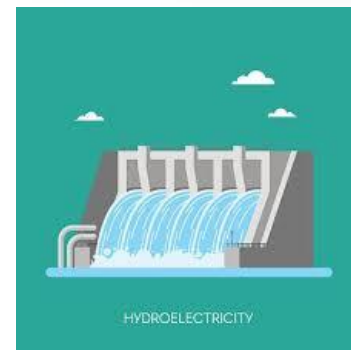
North Island
Demand : 1650 MW



Ignoring transmission losses,
net free reserve, HVDC ramp
up, HVDC capacity, reserve
sharing and reserve
requirement in SI

Energy CVP = 10k
FIR CVP = 4.5k
SIR CVP = 4.5k

South Island
Demand : 1000 MW



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Case Study 1 example

North Island

Demand : 1650 MW



Energy price: \$9000.01/MWh **350 MW**

IL FIR : **100 MW** @ 100 \$/MWh

IL SIR : **100 MW** @ 200 \$/MWh

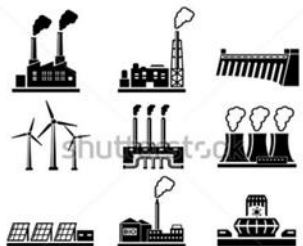
FIR price: \$4.5k/MWh **50 MW FIR deficit**

SIR price: \$4.5k/MWh **50 MW SIR deficit**

ENRG: **1300 MW** @ 100\$/MWh

FIR : **200 MW** @ 20 \$/MWh

SIR : **200 MW** @ 30 \$/MWh



HVDC
NI ← SI

South Island

Demand : 1000 MW

ENRG: **1350 MW** @ 0.01\$/MWh



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Case Study 2

Skip example

- Three supply sources (A, B, C) are constrained by either reserve class

$$Price_{energy} = \frac{1}{3} (Cost_{energyA} + Cost_{energyB} + Cost_{energyC} + Cost_{FIR} + Cost_{SIR})$$

- Assuming FIR supply is constrained (scarce).

$$Price_{energy} = \frac{1}{3} (Cost_{energyA} + Cost_{energyB} + Cost_{energyC} + CVP_{FIR} + Cost_{SIR})$$

- Assuming $CVP_{FIR} = \$10,000/\text{MWh}$, marginal energy cost at A, B and C is insignificant and marginal SIR price is very low $\rightarrow Price_{energy} \approx 3333.33$

\rightarrow Energy supply source with marginal cost > 3333.33 will not be cleared but a reserve deficit is preferable by the model.

Case Study 2 example

North Island

Demand : 1510 MW



Ignoring transmission losses,
net free reserve, HVDC ramp
up, HVDC capacity, reserve
sharing and reserve
requirement in SI

Energy CVP = 10k

FIR CVP = 10k

SIR CVP = 10k

South Island

Demand : 1000 MW



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Case Study 2 example

North Island

Demand : 1510 MW



ENRG: 350MW @ 0.01\$/MWh

FIR : 20MW @ 1\$/MWh

SIR : 30MW @ 1\$/MWh



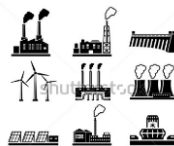
ENRG: 350MW @ 0.02\$/MWh

FIR : 20MW @ 2\$/MWh

SIR : 30MW @ 2\$/MWh



ENRG: 100MW @ 5k\$/MWh



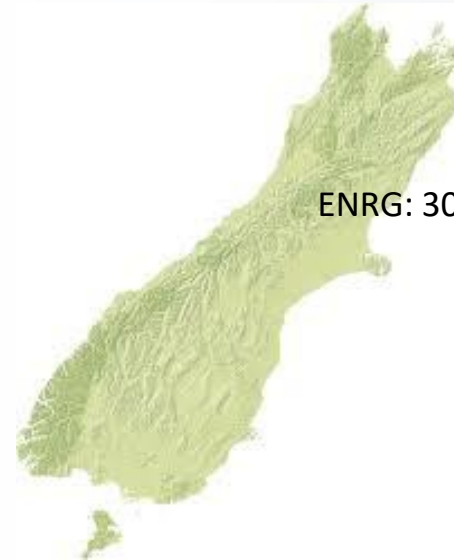
ENRG: 1000MW @ 100\$/MWh

FIR : 200MW @ 3\$/MWh

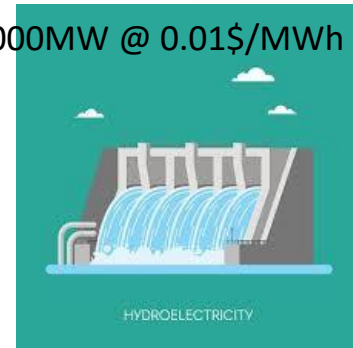
SIR : 300MW @ 3\$/MWh

South Island

Demand : 1000 MW



ENRG: 3000MW @ 0.01\$/MWh



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Case Study 2 example

North Island

Demand : 1510 MW



ENRG: 230MW @ 0.01\$/MWh

FIR : 20MW @ 1\$/MWh

SIR : 30MW @ 1\$/MWh



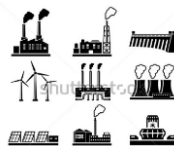
ENRG: 230MW @ 0.02\$/MWh

FIR : 20MW @ 2\$/MWh

SIR : 30MW @ 2\$/MWh



ENRG: 0MW @ 5k\$/MWh



ENRG: 800MW @ 100\$/MWh

FIR : 200MW @ 3\$/MWh

SIR : 200MW @ 3\$/MWh

HVDC
NI ← SI
250 MW

South Island

Demand : 1000 MW

ENRG: 1250MW @ 0.01\$/MWh



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Case Study 2 example

North Island

Demand : 1510 MW



ENRG: 230MW @ 0.01\$/MWh

FIR : 20MW @ 1\$/MWh

SIR : 30MW @ 1\$/MWh



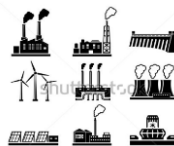
ENRG: 230MW @ 0.02\$/MWh

FIR : 20MW @ 2\$/MWh

SIR : 30MW @ 2\$/MWh



ENRG: 0MW @ 5k\$/MWh



ENRG: 800MW @ 100\$/MWh

FIR : 200MW @ 3\$/MWh

SIR : 200MW @ 3\$/MWh

HVDC

NI ← SI

250 MW

Energy price: \$3334.35/MWh

FIR price: \$10k/MWh

SIR price: \$3/MWh

10 MW of FIR deficit

South Island

Demand : 1000 MW

ENRG: 1250MW @ 0.01\$/MWh



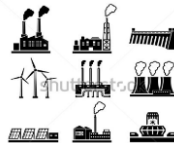
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Case Study 2 example

North Island

Demand : 1650 MW



Ignoring transmission losses,
net free reserve, HVDC ramp
up, HVDC capacity, reserve
sharing and reserve
requirement in SI

Energy CVP = 10k

FIR CVP = 15k

SIR CVP = 15k

South Island

Demand : 1000 MW



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Case Study 2 example

North Island

Demand : 1510 MW



ENRG: 220MW @ 0.01\$/MWh

FIR : 20MW @ 1\$/MWh

SIR : 30MW @ 1\$/MWh



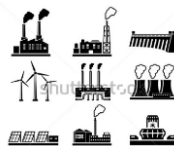
ENRG: 220MW @ 0.02\$/MWh

FIR : 20MW @ 2\$/MWh

SIR : 30MW @ 2\$/MWh



ENRG: 30MW @ 5k\$/MWh



ENRG: 800MW @ 100\$/MWh

FIR : 200MW @ 3\$/MWh

SIR : 190MW @ 3\$/MWh

HVDC

NI ← SI

240 MW

Energy price: \$5000/MWh

FIR price: \$14,996.96k/MWh

SIR price: \$3/MWh

South Island

Demand : 1000 MW

ENRG: 1240MW @ 0.01\$/MWh



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Issues with current reserve scarcity modelling

- If reserve CVPs too low → available expensive supply may not be used but risk violation is preferred if there are multiple risk setters.
- If reserve CVPs too high → energy violation might be preferable by SPD model instead of violating reserve requirement and “keeping the lights on”

Desirable outcomes during scarcity in real time pricing

- Reserve/risk violation is preferable to load shedding.
 - Reserve/risk violation should be limit at certain level.
 - Reserve price reflecting the risk(s) that are covered.
-
- The current reserve scarcity modelling can't achieve all of the above.

Proposed risk/reserve modelling

HVDC risk :

$$IslandRisk_{i,c,rc} = HVDCRec_i - RiskOffset_{i,c,rc} - \mathbf{RiskViolation}_{i,c,rc}$$

$$\forall c \in RESERVECLASSES \forall i \in ISLANDS \forall rc \in \{DCCEi, DCECEi\}$$

Generation risk :

$$\begin{aligned} & IslandRisk_{i,c,rc} \\ &= Generation_g - RiskOffset_{i,c,rc} + Reserver_g, c - \mathbf{RiskViolation}_{i,c,rc} \end{aligned}$$

$$\forall g \in ISLANDRISKGENERATORS_i \forall c \in RESERVECLASSES$$

$$\forall i \in ISLANDS \forall rc \in \{ACCERISKSi, AECERISKSi\}$$

Proposed risk/reserve modelling

Matching of requirements and availability:

$$IslandRisk_{i,c,rc} \leq IslandReserve_{i,c} + \cancel{ReserveDeficit_{i,c}}$$
$$\forall i \in ISLANDS \quad \forall c \in RESERVECLASSES \quad \forall rc \in RISKCLASSES$$

Total cleared reserve:

$$IslandReserve_{i,c} = \sum_{r \in RESERVEOFFERS_{i,c}} Reserve_r$$
$$\forall c \in RESERVECLASS \quad \forall i \in ISLANDS$$

Proposed risk/reserve modelling

Matching of requirements and availability:

$$IslandRisk_{i,c,rc} \leq \sum_{r \in RESERVEOFFERS_{i,c}} Reserve_r + \text{ReserveDeficit}_{i,c}$$

$$\forall i \in ISLANDS \quad \forall c \in RESERVECLASSES \quad \forall rc \in RISKCLASSES$$

Risk Violation Tranches Allocation:

$$RiskViolation_{i,c,rc} = \sum_{j \in VIOLATIONTRANCHES} RiskViolationTranches_{i,c,rc,j}$$

$$RiskViolationTranches_{i,c,rc,j} \leq RiskViolationTrancheLimits_{i,c,rc,j}$$

$$\forall i \in ISLANDS \quad \forall c \in RESERVECLASSES \quad \forall rc \in RISKCLASSES$$

Proposed risk/reserve modelling

Objective function:

Net Benefit

$$\begin{aligned} &= \textit{DemandBenefit} - \textit{GenerationCosts} - \textit{ReserveCost} \\ &- \textit{EnergyShortageCost} - \textit{ReserveDeficitCost} \\ &- \textbf{\textit{RiskViolationCost}} - \textit{OtherViolationCost} \end{aligned}$$

Proposed risk/reserve modelling

$$EnergyShortageCost = \sum_{i,j} EnergyShortage_{i,j} \times EnergyCVP_j$$

$$\cancel{ReserveDeficitCost} = \sum_{i,\epsilon} \cancel{ReserveDeficit_{i,\epsilon}} \times \cancel{ReserveCVP_{\epsilon}}$$

$$RiskViolationCost = \sum_{i,c,rc,j} RiskViolationTranches_{i,c,rc,j} \times RiskCVP_{c,j}$$

$\forall i \in ISLANDS \quad \forall j \in VIOLATIONTRANCHES$

$\forall c \in RESERVECLASSES \quad \forall rc \in RISKCLASSES$

Example of Risk Violation Tranche Limits and CVPs

Violation limits (MW)	FIR CVP (\$/MWh)	SIR CVP (\$/MWh)
10 MW	4500	4000
10 MW	7500	7000
10 MW	9500	9000
20 MW	12000	11000
1000 MW	15000	15000

Case Study 1

- One risk setter and both reserve classes constrained.
 - Assuming $CVP_{\text{engy}} = \$10,000/\text{MWh}$ and the risk binding supply source is cheap enough
- Can violate the risk up to 10 MW before load shedding occurs.

Case Study 2

- Three supply sources (A, B, C) are constrained by 6s reserve class (FIR)
 - Assuming $CVP_{\text{engy}} = \$10,000/\text{MWh}$ and the risk binding supply sources are cheap enough
 - Assuming the other non-risk setting supply sources are available at \$5000/MWh
- Risk violation up to 10 MW occurs at A, B, C in the order of energy cost and free up 30 MW of energy before the \$5000/MWh supply is required.

CONCLUSION

- The multi-step risk violation model seems to do the tricks.
- Still have to decide on the limits and cost of risk violation tranches.